## Double and Triple Integral Practice

1. Find the volume of the solid region bounded by y=0, y=3,  $z=x^2$ , and  $z=2-x^2$ .



2. Use polar or cylindrical coordinates to find the volume of the solid inside the sphere  $x^2 + y^2 + z^2 = 9$  and above the cone  $z = \sqrt{x^2 + y^2}$ .

3. Use spherical coordinates to find the volume of the solid inside the sphere  $x^2 + y^2 + z^2 = 9$  and above the cone  $z = \sqrt{x^2 + y^2}$ .

4. Find the average value of  $f(\rho, \phi, \theta) = \rho$  over the ball  $\rho \le 1$ .

5. A 1-inch radius cylindrical hole is drilled through the center of a ball with 2-inch radius. Find the volume of the core that was removed from the ball.



6. Find the area inside the circle  $x^2 + (y-2)^2 = 4$  that is outside the circle  $x^2 + y^2 = 8$ . Hint:  $\sin^2 \theta = \frac{1}{2} - \frac{1}{2}\cos 2\theta$ .

