Poisson and Binomial practice problems

- 1. Customers arrive at a checkout counter in a department store according to a Poisson distribution at an average of 7 per hour.
  - a. Probability that exactly five customers arrive in the next hour?
  - b. Probability that no more than three customers arrive in the next hour?
  - c. Probability that at least two customers arrive in the next hour?

2. A random sample of 20 gadgets from a production line during an hour are tested. When the plant is functioning normally about 1% of gadgets fail the test. A large number of failures is evidence that something is wrong. The question is, what is a large number? To get a sense of how many failures might be worrisome, fill in the table below, where the random variable *X* is how many gadgets failed out of the 20 tested.

| j      | 0 | 1 | 2 | 3 | 4 |
|--------|---|---|---|---|---|
| P(X=j) |   |   |   |   |   |

3. A salesperson has found that the probability of a sale on a single contact is approximately 0.03. If the salesperson contacts 100 prospects, what is the probability of making at least one sale? Calculate in two ways: **exactly** (clearly stating the distribution you use) and **approximately** (again clearly specify what distribution you use).